

1797

EE740

10-10

9-10

3-10

4-20

5-20

6-30

100

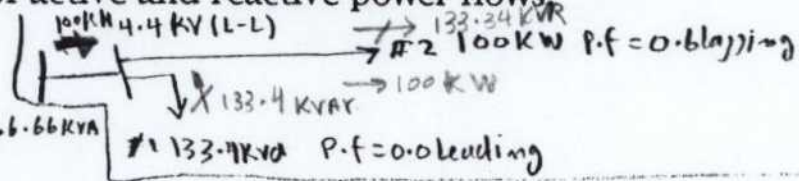
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Department of Electrical
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Problem 1. A ~~three~~ ^{three} phase distribution feeder has two loads : Load #1 is rated 133.4 kva with power factor of 0.0 leading. Load #2 is rated 100 kW with power factor of 0.6 lagging. Both loads are connected to the same load bus. If the load voltage is to be maintained at 4.4 kV (line value), compute the power factor at the load bus and the direction of active and reactive power flows.



$$P = S \cos \theta$$

$$S = \frac{P}{\cos \theta} = \frac{100}{0.6} = 166.66 \text{ kVA}$$

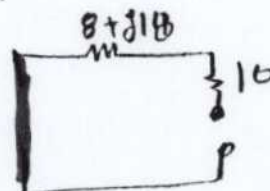
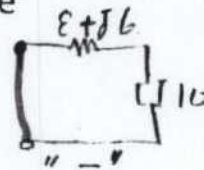
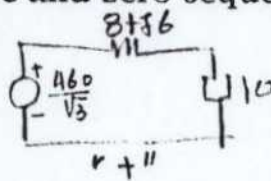
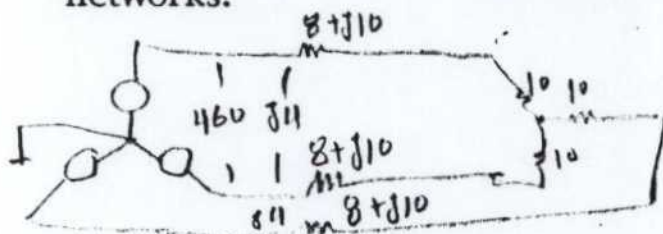
$$S_1 = 166.66 \angle 53.13^\circ \text{ kVA}$$

$$= 100 \text{ kW} + j 133.34$$

$$S_2 = 133.34 \angle -90^\circ = 0 - j 133.34$$

$$S_{\text{Total}} = 100 \text{ kW} + j 133.34 - j 133.34 = 100 \text{ kW} \quad P.f = 1$$

Problem 2. A balanced wye connected generator rated 460 volts (line Value) is supplying a balanced wye connected resistive load of 10 ohms through a balanced transmission line with $Z_s = 8 + j10$, $Z_{ab} = Z_{bc} = Z_{ca} = Z_m = j4$ (ohms). If the generator is grounded and load is not grounded, draw the positive, negative and zero sequence networks.



$$Z_0 = Z_s + 2Z_m = 8 + j18$$

$$Z_1 = Z_s - Z_m = 8 + j10 - j4$$

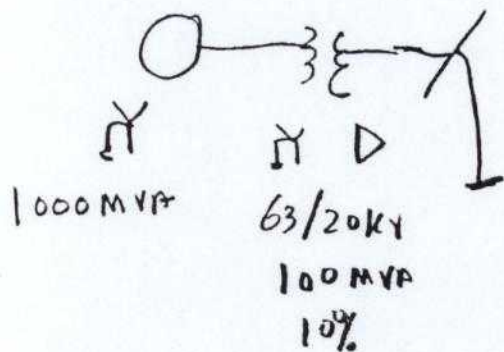
$$Z_2 = Z_s - Z_m = 8 + j6$$

Problem 3 Same as problem 2, but both the generator and loads are grounded. Compute the symmetrical components of currents.

$$I_1 = \frac{265.84 \angle 0^\circ}{18 + j6} = \frac{265.84 \angle 0^\circ}{18.97 \angle 18.4^\circ} = 14 \angle -18.4^\circ$$

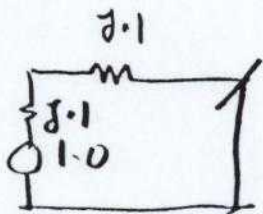
$$I_2 = 0 \quad I_0 = 0$$

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Problem 4. A three phase transformer rated 63 kV (wye connected and grounded)/20 kV(delta connected), 100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. Assume a balanced three phase fault on 20 kV side while the 63 kV side is supplied from the power system at the rated voltage. Compute the short circuit capacity of 20 kV bus.



$$SCC_{p.u} = \frac{1000}{100} = 10$$

$$X_{th} = \frac{1}{10} = 0.1$$

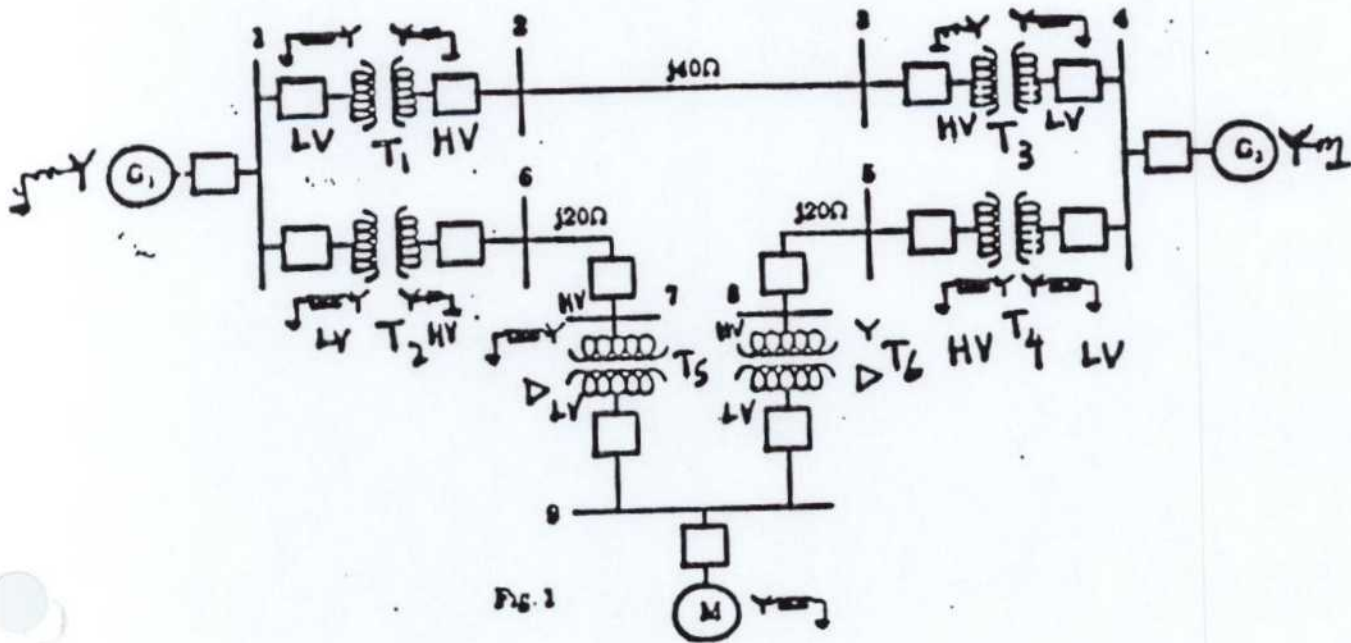


$$I_f = \frac{1}{j0.2} = 5 \text{ p.u.}$$

$$S.C.C. \text{ p.u.} = 5 \text{ p.u.}$$

$$S.C.C. \text{ MVA} = 5 \times 100 = 500 \text{ MVA}$$

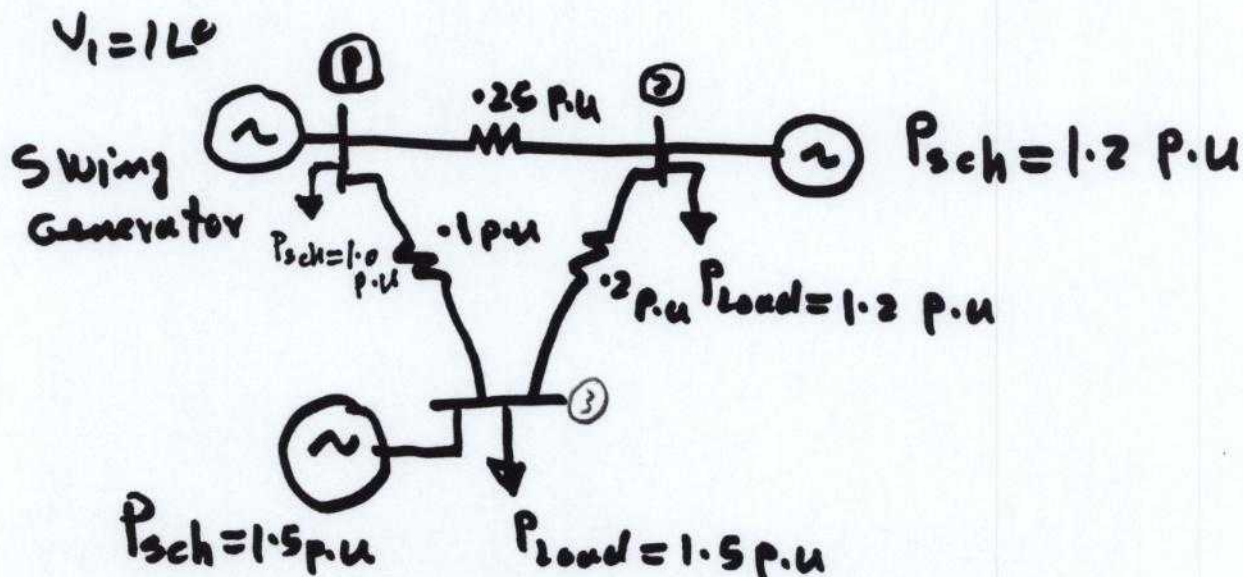
Problem 1. Consider the power system given below. Assume the following cases: Case 1): two phases are short circuited at bus 2 and then connected to ground. Case 2): one phase connected to ground at the mid section of 20 ohm transmission line between bus 6 and bus 7. Case 3): three phases are short circuited at bus 5 and then connected to ground. Determine whether the ground current will flow by indicating "yes" or "no" in the Table given below.



| Location | Case1 | Case 2 | Case 3 |
|------------------------------------------|-------|--------|--------|
| Ground reactance of trans. T3 on LV side | yes | yes | NO |
| Ground reactance of of generator G1 | yes | yes | NO |
| Ground reactance of motor M | NO | NO | NO |
| Ground reactance of generator G2 | yes | yes | NO |
| Ground reactance of trans.T4 on HV side | NO | NO | NO |

Problem 4: A three phase transformer rated 63 kV (grounded wye) /20 kV(delta) ,100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. Assume a balanced three phase fault on 20 kV side while the 63 kV side is supplied from the power system at the rated voltage. Compute the short circuit capacity of 20 kV bus.

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Problem 5. for the power system given below:



- 1) Compute Y_{bus} model
- 2) compute Jacobian matrix
- 3) compute ΔP_2 and ΔP_3 . Use one iteration only
- 4) Compute transmission line losses.
- 5) compute the swing generator power supplied to the network.

$$Y_{bus} = \begin{bmatrix} 14 & -4 & -10 \\ -4 & 9 & -5 \\ -10 & -5 & 15 \end{bmatrix}$$

$$I_{bus} = Y_{bus} V_{bus}$$

$$V_1 = 1 \angle 0$$

$$0 = V_2 I_2^*$$

$$0 = V_3 I_3^*$$

$$I_2^* = 0$$

$$I_3^* = 0$$

$$V_2 = 1 \angle 0$$

$$V_3 = 1 \angle 0$$

$$\Delta P_2 = 0$$

$$\Delta P_3 = 0$$

$$J = \begin{bmatrix} 9 & -5 \\ -5 & 15 \end{bmatrix}$$

$$P_1 = 1.0 \text{ p.u.}$$

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Final

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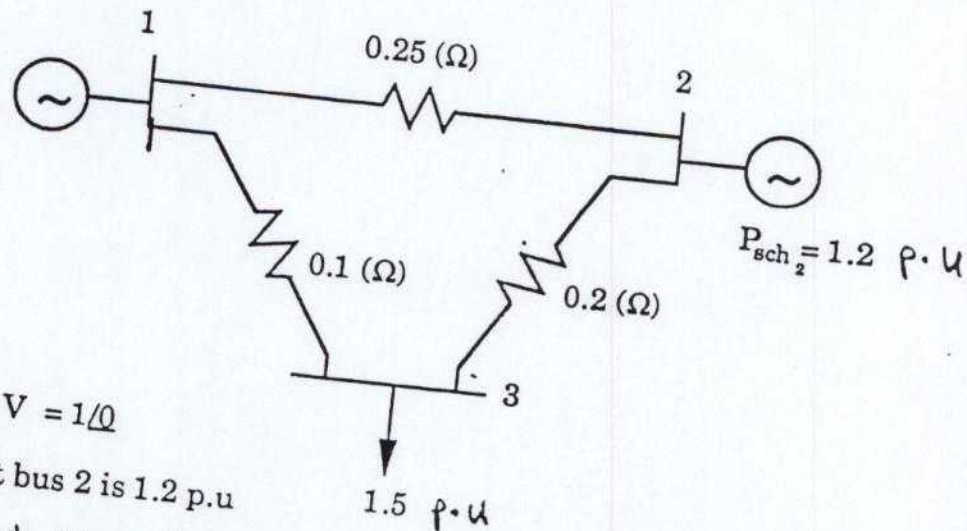
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Department of Electrical Engineering
The Ohio State University

Fall 2000

Problem 7

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Given:

- Bus 1 is slack bus: $V = 1 \angle 0$
- Scheduled power at bus 2 is $1.2 \, \text{p.u.}$
- Scheduled Load at Bus 3 is $1.5 \, \text{p.u.}$

Compute:

- 1) Y Bus model
- 2) Bus voltages using Gauss-Seidel method
- 3) Power mismatch at bus 2 and bus 3
- 4) Power supplied by the swing bus
- 5) Power Loss of transmission lines.

Problem 3. A three phase transformer rated 138 kV (grounded wye) /13.8 kV(grounded wye),100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. The power system bus voltage is 138 kV. The 13.8 kV side of transformer is fully loaded with a power factor of 0.8 lagging at rated voltage. Compute the fault current for a single line to ground fault at 13.8 kV bus for the following conditions: a) if the load is connected as a grounded wye . b) if the load is connected as an ungrounded wye . Assume that the impedance of positive, negative and zero sequence networks are equal.

FINAL

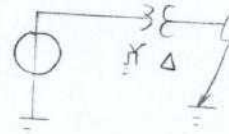
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Problem 1. A three phase transformer rated 63 kV (grounded wye) / 20 kV(delta), 100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. Assume a balanced three phase fault on 20 kV side while the 63 kV side is supplied from the power system at the rated voltage. Compute the short circuit capacity of 20 kV bus.

Choose base values as

$$S_b = 100 \text{ MVA}$$

$$V_{b,H} = 63 \text{ KV} \quad V_{b,L} = 20 \text{ KV}$$

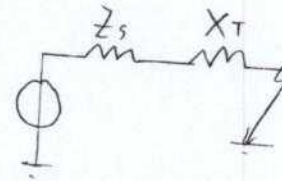


So the short circuit capacity of the system is

$$SCC = \frac{1000}{100} = 10 \text{ p.u.}$$

The Impedance of the system is

$$Z_s = \frac{1}{SCC} = 0.1 \text{ p.u.}$$



The reactance of the transformer is

$$X_T = 0.1 \text{ p.u.}$$

when a 3 ϕ short occurs at low voltage side of transformer

$$Z_{eq} = Z_s + X_T = 0.1 + 0.1 = 0.2$$

So the short circuit capacity is

$$SCC_{20KV} = \frac{1}{Z_{eq}} = 5 \text{ p.u.}$$

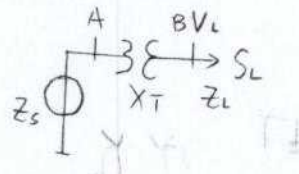
$$\text{or } SCC_{20KV} = 5 \times 100 = 500 \text{ MVA}$$

Problem 2. A three phase transformer rated 138 kV (grounded wye) / 13.8 kV (grounded wye), 100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. The power system bus voltage is 138 kV. The 13.8 kV side of transformer is fully loaded with a power factor of 0.0 lagging at rated voltage. Compute the fault current for a single line to ground fault at 13.8 kV bus for the following conditions: a) if the load is connected as a grounded wye. b) if the load is connected as an ungrounded wye. Assume that the impedance of positive, negative and zero sequence networks are equal.

Choose base values as

$$S_b = 100 \text{ MVA}$$

$$V_{b,H} = 138 \text{ kV}, \quad V_{b,L} = 13.8 \text{ kV}$$

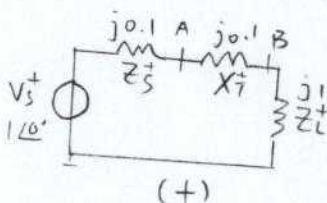


System impedance $Z_s = \frac{1}{SCC} = \frac{1}{\frac{1000}{10^3}} = 0.1 \text{ pu}$

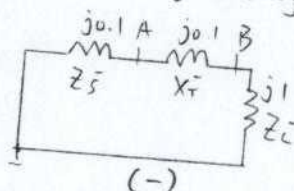
transformer impedance $X_T = 0.1 \text{ p.u.}$

load impedance $Z_L = \frac{|V_L|^2}{S_L^*} = \frac{1}{(1 \angle 90^\circ)^*} = j1 \text{ pu.}$

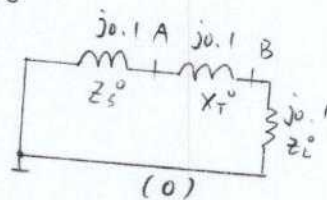
a) the load is connected as a grounded wye.



(+)



(-)

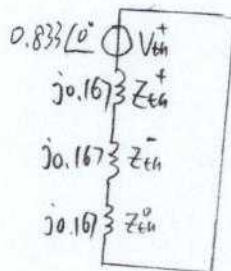


(0)

for bus B, $Z_{th}^+ = Z_{th}^- = Z_{th}^0 = j0.2 \parallel j1 = j0.167 \text{ pu.}$

$$V_{th}^+ = V_s^+ \frac{j1}{j1.2} = 0.833 \angle 0^\circ \text{ pu}$$

$$I^+ = I^- = I^0 = \frac{V_{th}^+}{Z_{th}^+ + Z_{th}^- + Z_{th}^0} = \frac{0.833 \angle 0^\circ}{3 \times j0.167} = -j1.67 \text{ p.u.}$$



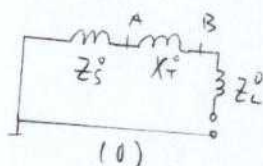
$$S_b \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} I^+ \\ I^- \\ I^0 \end{bmatrix} = \begin{bmatrix} -j5 \\ 0 \\ 0 \end{bmatrix} \text{ pu}$$

$$I_a = -j5 \times \frac{100 \times 10^6}{13.8 \times 10^3} = -j36.23 \times 10^3 \text{ A} = -j36.23 \text{ KA}$$

$$I_b = I_c = 0$$

b) the load is connected as an ungrounded wye.

the positive and negative sequence network are the same as in (a)



(0)

$$Z_{th}^0 = Z_s^0 + X_T^0 = j0.2$$

$$I^+ = I^- = I^0 = \frac{0.833 \angle 0^\circ}{j0.167 + j0.167 + j0.2} = -j1.56 \text{ p.u.}$$

$$S_b \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} I^+ \\ I^- \\ I^0 \end{bmatrix} = \begin{bmatrix} -j4.68 \\ 0 \\ 0 \end{bmatrix} \text{ pu}$$

$$I_b = I_c = 0$$

Problem 3 A three phase transformer rated 138 kV (grounded wye) / 13.8 kV (delta), 100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. The power system bus voltage is 138 kV. The 13.8 kV side of transformer is fully loaded with a power factor of 0.0 leading at rated voltage. Compute the fault current for a single line to ground fault at 13.8 kV bus for the following conditions: a) if the load is wye connected and grounded b) if the load is delta connected. Assume that the impedance of positive, negative and zero sequence networks are equal.

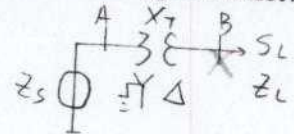
choose $S_b = 100 \text{ MVA}$

$V_{b,A} = 138 \text{ kV}$ $V_{b,B} = 13.8 \text{ kV}$

$Z_s = \frac{1}{S_{sc}} = \frac{1}{\frac{1000}{100}} = 0.1 \text{ p.u.}$

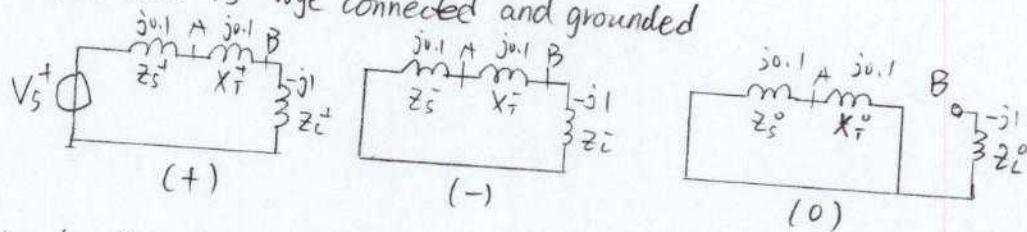
$X_T = 0.1$

$Z_L = \frac{|V_L|^2}{S_L^*} = -j1 \text{ p.u.}$



$S_L = 1 \angle -90^\circ$

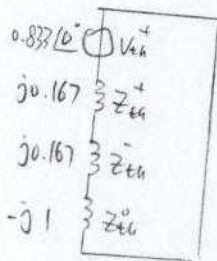
a) the load is wye connected and grounded



for bus B, $Z_{th}^+ = Z_{th}^- = j0.2 // j1 = j0.167 \text{ p.u.}$

$Z_{th}^0 = Z_L^0 = -j1$

$V_{th}^+ = V_s^+ \times \frac{j1}{j1.2} = 0.833 \angle 0^\circ \text{ p.u.}$

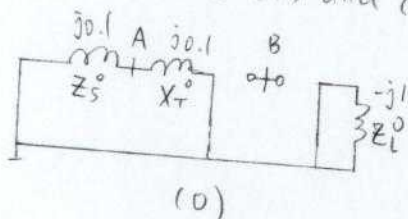


$I^+ = I^- = I^0 = \frac{V_{th}^+}{Z_{th}^+ + Z_{th}^- + Z_{th}^0} = \frac{0.833 \angle 0^\circ}{j0.167 + j0.167 - j1} = +j1.25 \text{ p.u.}$

$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & a^2 & a \\ 1 & a & a^2 \end{bmatrix} \begin{bmatrix} I^+ \\ I^- \\ I^0 \end{bmatrix} = \begin{bmatrix} +j3.75 \\ 0 \\ 0 \end{bmatrix} \text{ p.u.}$

$I_a = j3.75 \times \frac{100 \times 10^6}{13.8 \times 10^3} = j27.17 \text{ kA}$
 $I_b = I_c = 0$

b) the load is delta connected
the (+) and (-) sequence are the same as in a)



$Z_{th}^0 = \infty$

$I^+ = I^- = I^0 = \frac{V_{th}^+}{Z_{th}^+ + Z_{th}^- + Z_{th}^0} = 0$

$I_a = I_b = I_c = 0$

Problem 4 A transformer bank is composed of three single-phase transformers supplying a three-phase load consisting of three identical 100 Ohm reactors. Each single transformer, rated at 100 MVA, 138 kV/13.8 kV has a leakage reactance of 12%. The loads are connected in delta through a transmission line with $.1 + j.01$ Ohm impedance. Assume transformers are connected in wye/delta. Perform the following:
 A) Compute the single-phase equivalent circuit.
 B) Compute per unit equivalent circuit for a base of 100 MVA and a voltage base of 13.8 kV.

A) for transformer connected in Y/ Δ

$$V_H = \sqrt{3} \times 13.8 = 23.9 \text{ kV}$$

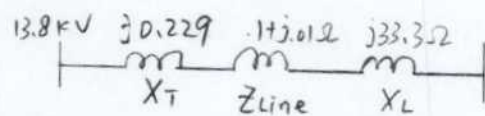
$$V_L = 13.8 \text{ kV}$$

$$\text{from LV side, } X_T = 0.12 \times \frac{(13.8 \times 10^3)^2}{100 \times 10^6} = 0.229 \Omega$$

the Y equivalent reactance of the load is

$$X_L = \frac{100}{3} = 33.3 \Omega$$

So the equivalent circuit for LV side is



from HV side, the equivalent circuit is

$$X_T = 0.229 \times \frac{23.9^2}{13.8^2} = 68.7 \Omega$$

$$Z_{line} = (.1 + j.01) \times \frac{23.9^2}{13.8^2} = 30 + j3 \Omega$$

$$X_L = 33.3 \times \frac{23.9^2}{13.8^2} = 9988 \Omega$$

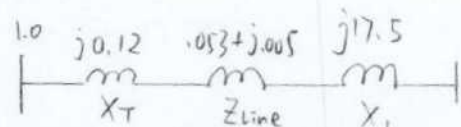
$$B) S_b = 100 \text{ MVA, } V_b = 13.8 \text{ kV}$$

$$Z_b = \frac{V_b^2}{S_b} = \frac{(13.8 \times 10^3)^2}{100 \times 10^6} = 1.9044$$

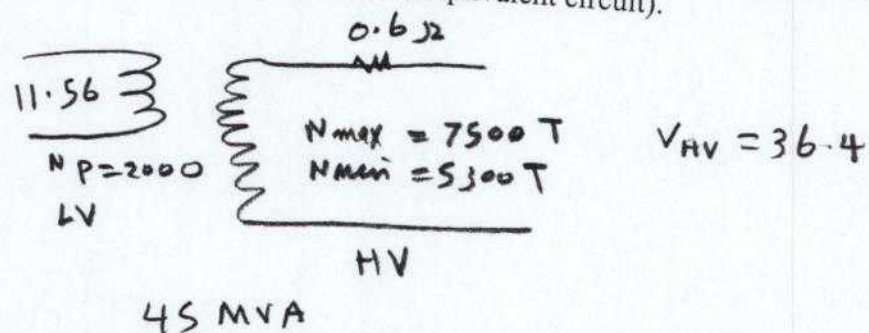
$$X_T = 0.12 \text{ p.u.}$$

$$Z_{line} = \frac{.1 + j.01}{1.9044} = .053 + j.005 \text{ p.u.}$$

$$X_L = \frac{33.3}{1.9044} = 17.5 \text{ p.u.}$$



Problem 1. A single-phase tap changing transformer has 2000 turns on the low voltage side and variable number of turns on the high voltage side ($N_{HV(max)} = 7500$ turns, $N_{HV(min)} = 5300$ turns). The transformer is connected to a power system with the low voltage of 11.56 kV and the high voltage of 36.4 kV. The transformer is rated at 45 MVA and the short circuit reactance referred to the high voltage side is equal to .6 ohm. Perform the following: a) Compute the per-unit equivalent circuit based on the tap setting of the high voltage side with $N_{HV} = 6000$ turns. b) the nominal turns of the high voltage side. (I do not want the PI equivalent circuit).



a)

$$N_{HV} = 6000 T$$

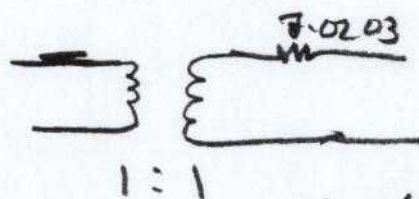
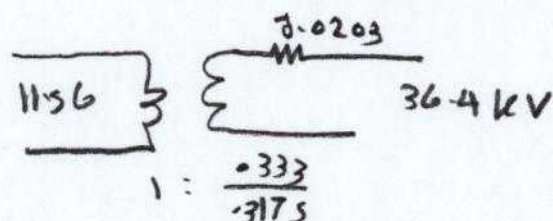
$$a = \frac{2000}{6000} = \frac{1}{3} = 0.333$$

$$b = \frac{11.56}{36.4} = 0.3175$$

$$c = \frac{a}{b} \neq 1$$

$$Z_{bHV} = \frac{V_{bH}^2}{S_b} = \frac{(36.4)^2}{45} = 29.44 \Omega$$

$$X_{p.u} = \frac{0.6}{29.44} = 0.0203 \text{ p.u.}$$

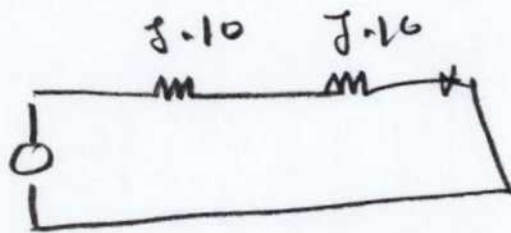


$$N = 6298$$

N_{max}

$$a = \frac{2000}{6298} = 0.3175$$

Problem 1. A three phase transformer rated 63 kV (grounded wye) /20 kV(delta) ,100 MVA and 10% short circuit reactance supplied from a grounded power system with short circuit capacity of 1000 MVA. Assume a balanced three phase fault on 20 kV side while the 63 kV side is supplied from the power system at the rated voltage. Compute the short circuit capacity of 20 kV bus.



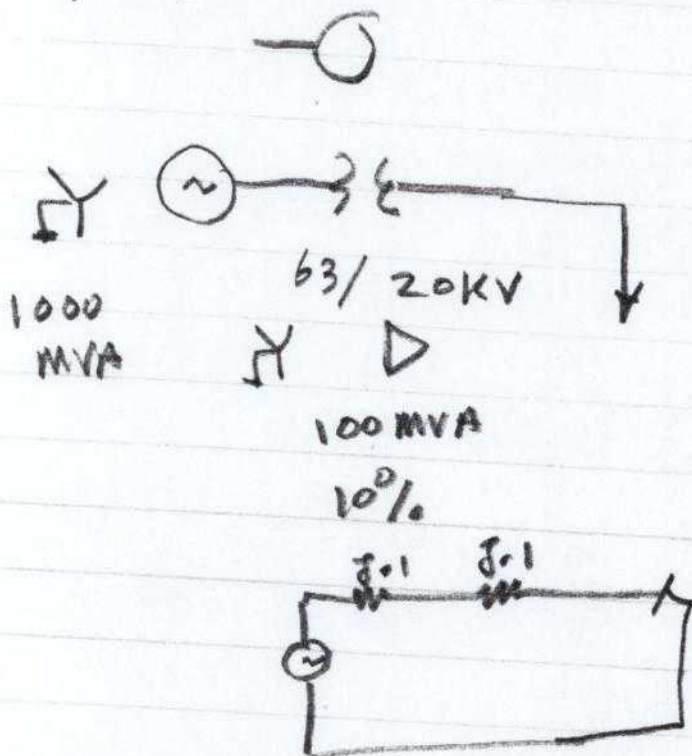
$$S.C.C. p.u = \frac{1000}{100} = 10$$

$$X_{th} = \frac{1}{10} = 0.1$$

$$S.C.C = \frac{1}{0.2} = 5 p.u$$

$$S.C.C = 500 MVA$$

Prob. 1



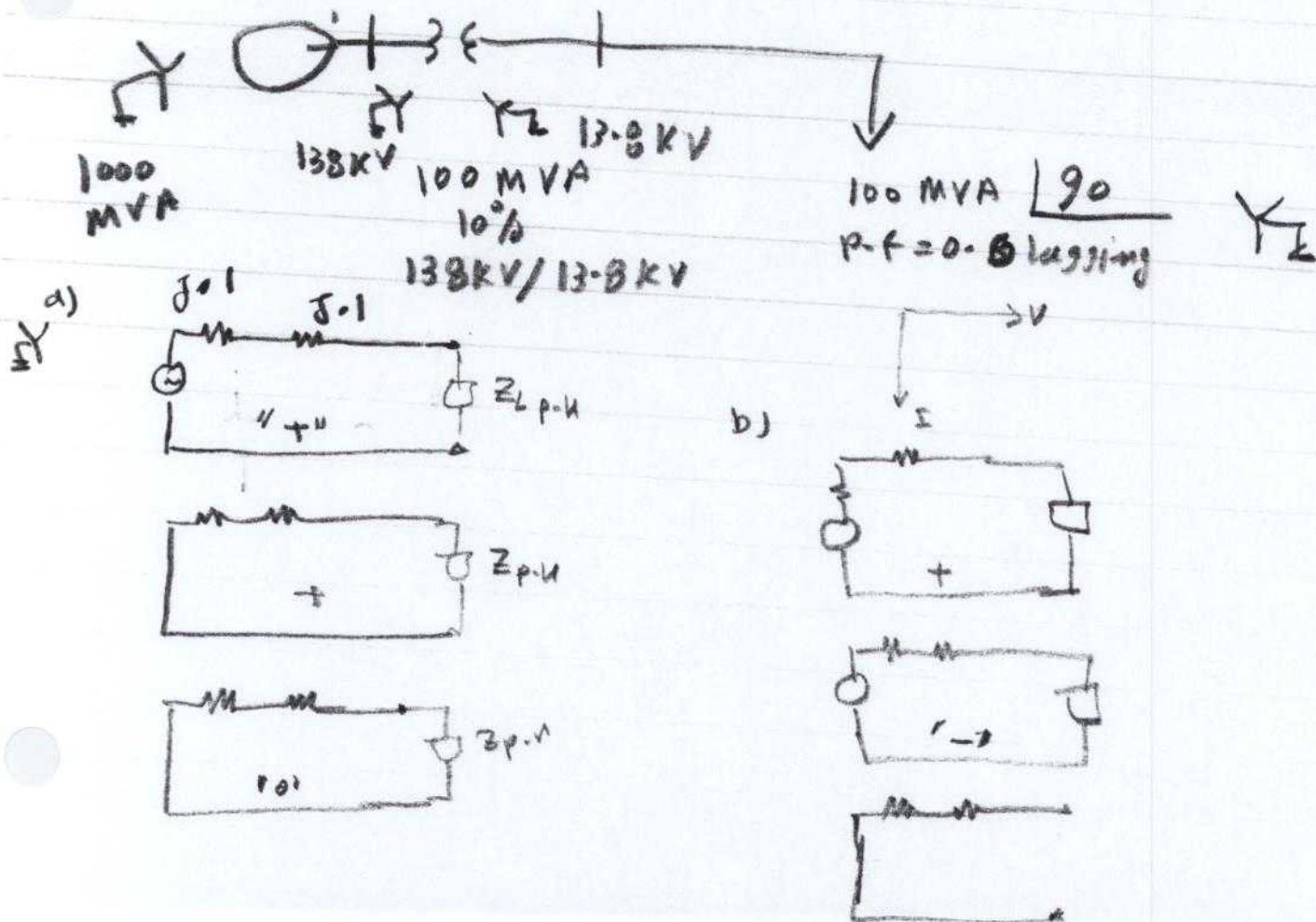
$$S_{C.C} \text{ p.u.} = \frac{1000}{100} = 10$$

$$X_{th} = \frac{1}{10} = 0.1$$

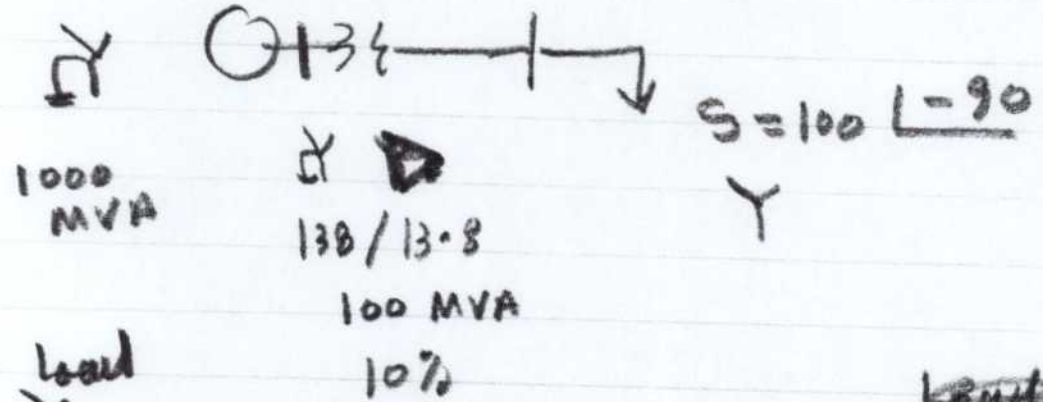
$$S.C.C_{pu} = \frac{1}{0.2} = \frac{5}{1} \text{ p.u.}$$

$$S.C.C = 500 \text{ MVA}$$

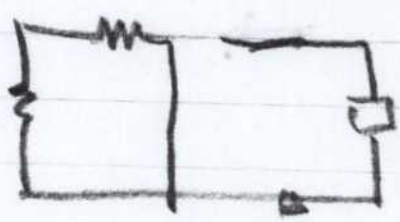
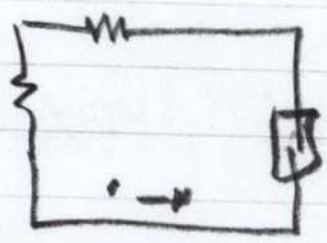
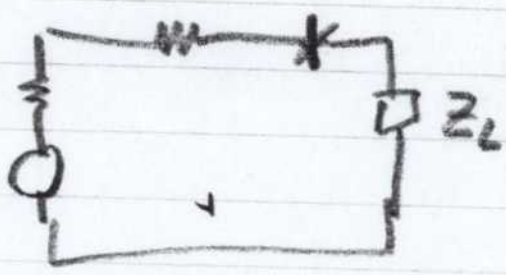
Prob. 2



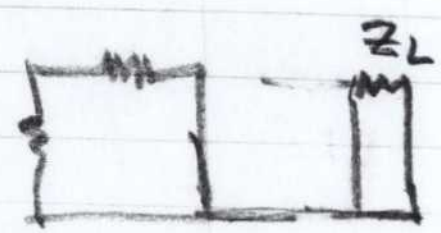
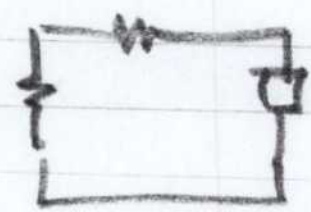
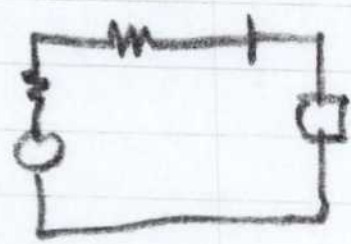
138KV



Load
Y



~~Load - Y~~
Load Δ



EE740

Name-----

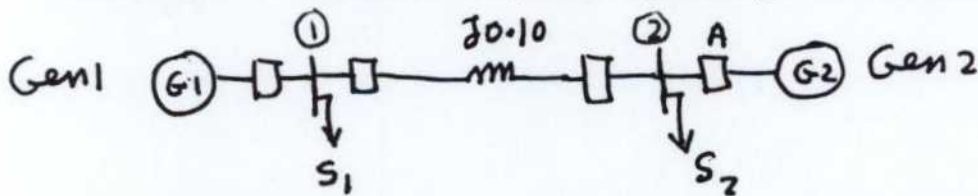
pledge "No aid given,
received, or observed"

Department of Electrical
Engineering

The Ohio State University

EE 740 -- Midterm Exam

Problem 1. Consider a power system given below.



The internal impedance of generators is: $Z_{g1} = j 0.10$

$Z_{g2} = j 0.20$ All values are in p.u.

- 1.) Compute YBUS model for power flow studies.
- 2.) Compute ZBUS model for short circuit studies.

Problem 2. For Problem 1, assume the following load and generation schedules:

Loads: $S_1 = 0.5 + j0.5$ p.u., $S_2 = 0.2 - j0.5$ p.u.

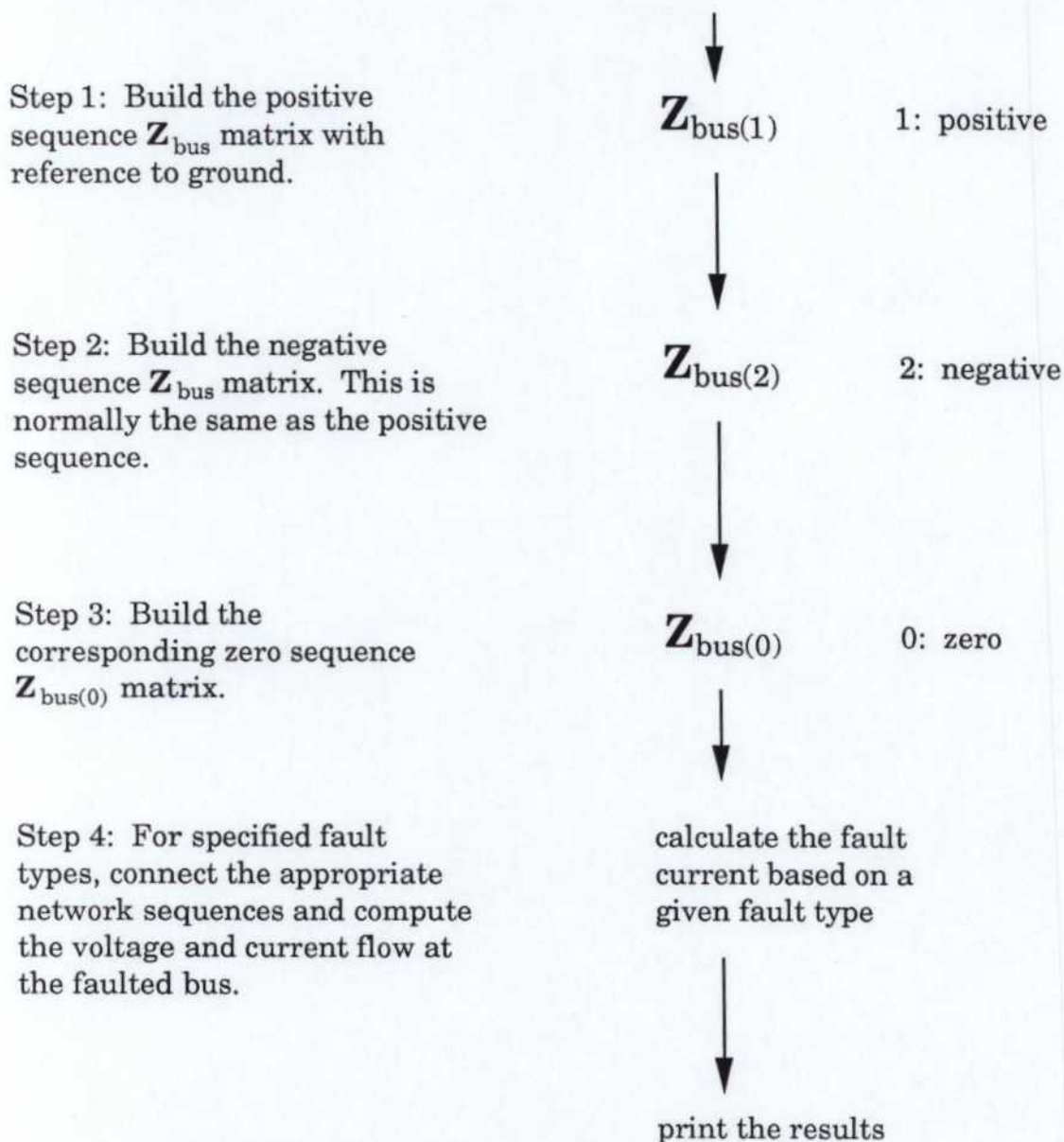
Generators: Generator one is the Swing generator and generator 2 scheduled power is $P=0.5$ p.u.

Use Gauss-Seidel and compute Load Voltage at BUS 2.

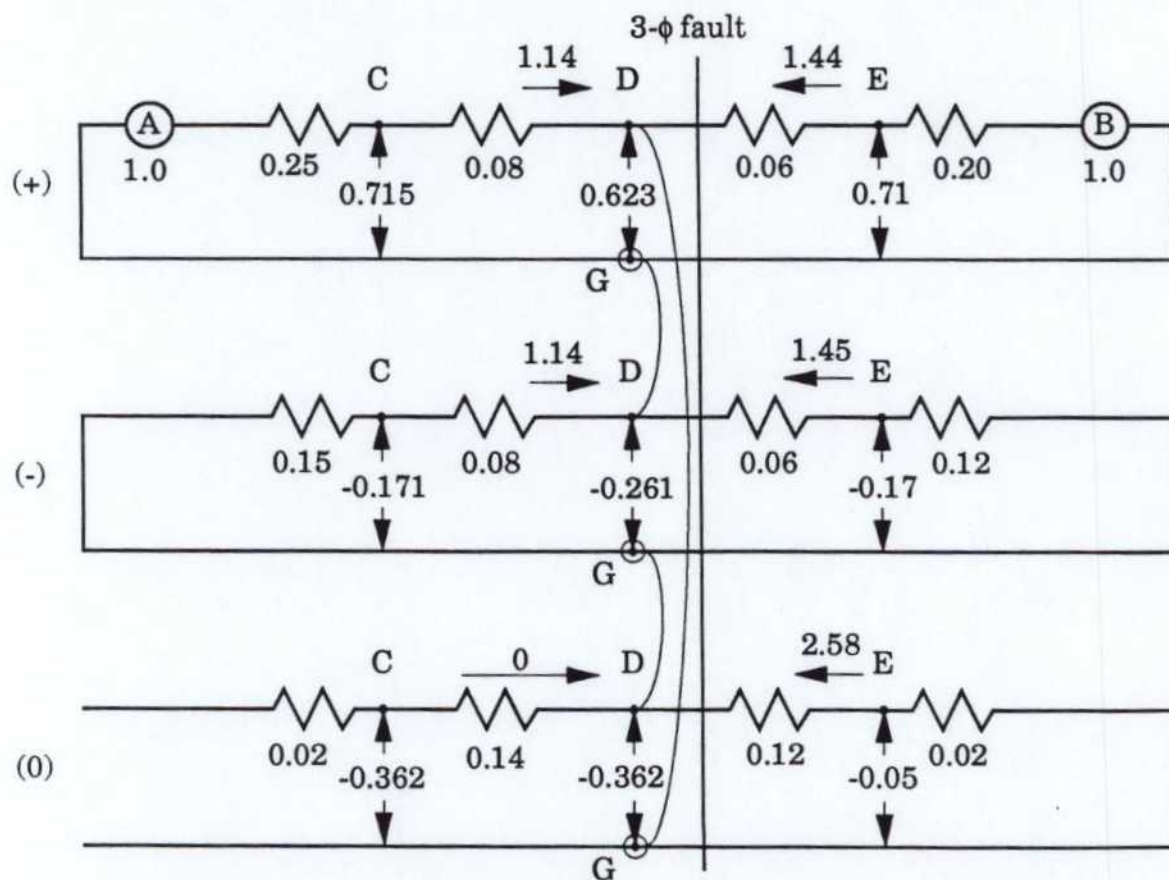
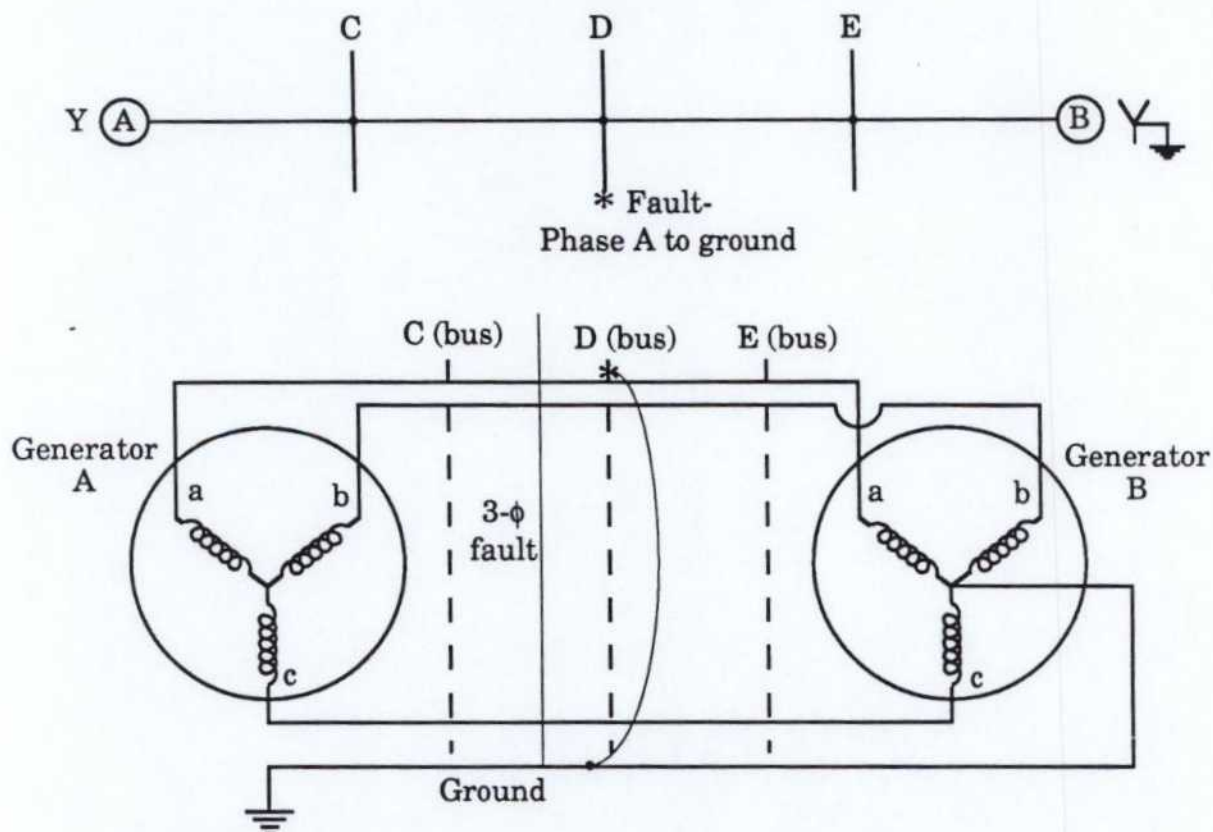
Assume $V_1 = 1.10$ p.u. (Give your results for one iteration only.)

Problem 3. For Problem 1; assume a three phase fault at BUS 2. Compute the fault current seen by circuit breaker A. *Ignore the loads.*

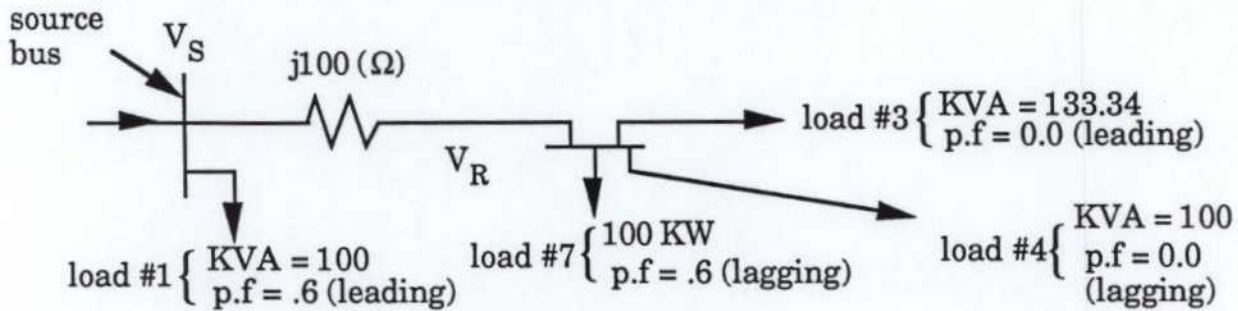
Algorithm for calculations of balanced and unbalanced fault currents.



EE740



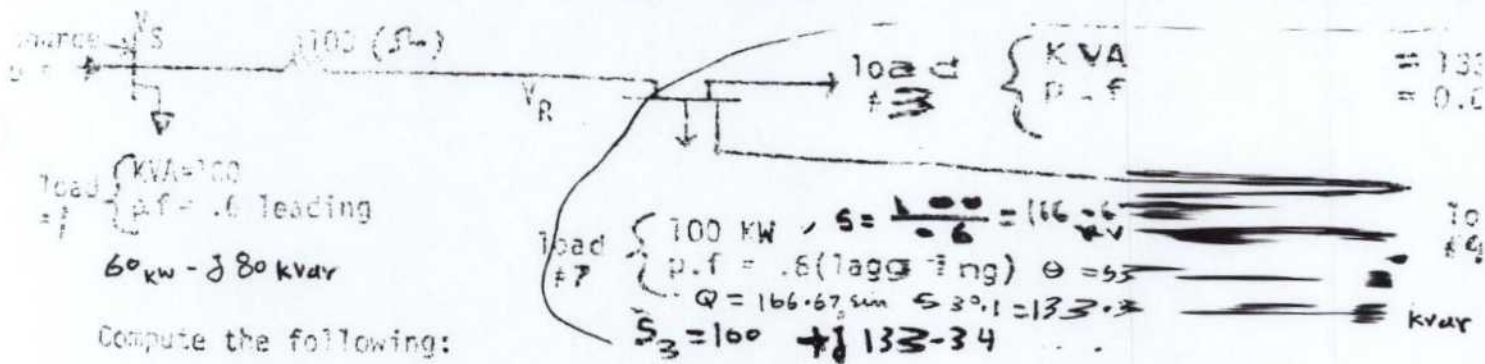
Problem 1. Consider a 3- ϕ distribution feeder as shown below:



Compute the following:

- 1) The source voltage V_S , if V_R is to be maintained at 4.4 V ($V_R = 4.4$ kV line value).
- 2) The source current and power factor at the source.
- 3) The total complex power supplied by the source
- 4) How much reactive power should be connected to the source bus for obtaining unity power factor at the source bus?

Problem 1. Consider a 3-phase distribution feeder as shown below:



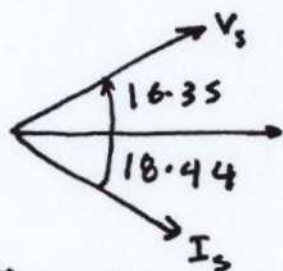
- 1) The source voltage V_s , if V_R is to be maintained at 4.4 kV .
- 2) The source current and power factor at the source.
- 3) The total complex power supplied by the source.
- 4) How much reactive power should be connected to the source to obtain unity power factor at the source?

$$1) \tilde{V}_{s-L} = (3100) \tilde{I}_{L-R} + 2543 \angle 0^\circ$$

$$\tilde{S}_R = \sqrt{3} \tilde{V}_{L-L} \tilde{I}_{L-R}^* \quad \tilde{I}_{L-R} = \frac{(100 + j100)}{\sqrt{3} \cdot 4.4 \angle 0} = 13.14 \angle -13.1^\circ$$

$$\tilde{V}_{s-L} = 4.02 \angle 16.35^\circ \text{ KV (L-L)} \quad \tilde{V}_{s-L-L} = 6.95 \angle 16.35^\circ$$

$$2) \tilde{I}_s = \tilde{I}_{L1} + \tilde{I}_{L2} \quad \tilde{I}_{L1} = \frac{(\tilde{S}_1)^*}{\sqrt{3} \tilde{V}_{s-L-L}} = \frac{(100 - j133.3)^*}{\sqrt{3} \cdot 6.95} = 16.9 \angle -18.44^\circ \text{ A}$$



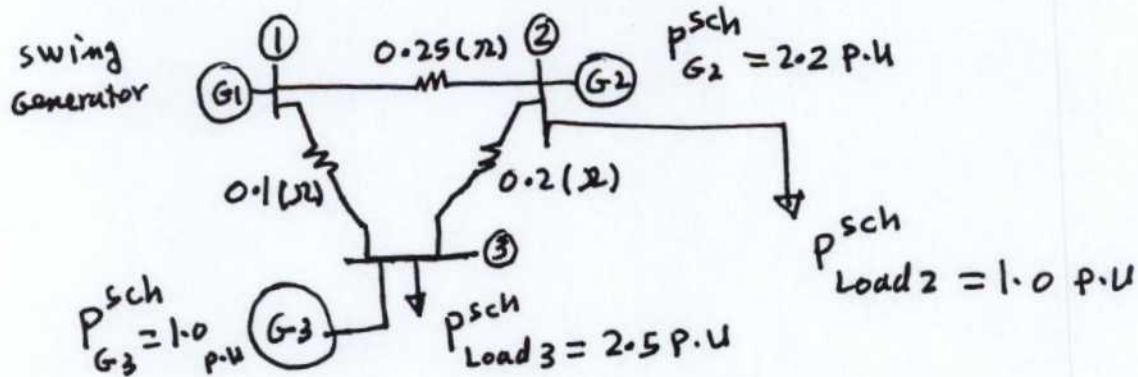
$$\text{p.f.}_s = \cos(16.35^\circ - (-18.44^\circ)) = \cos(34.79^\circ) = 0.82$$

$$3) \tilde{S}_s = \sqrt{3} \tilde{V}_{s-L-L} \tilde{I}_s^* = 201.18 \angle 34.8^\circ$$

$$= 165.2 + j114.82 \text{ kVA}$$

$$4) \tilde{S}_c = -j114.82 \text{ kVAR}$$

Problem 4. For the power system given below:



1.) Assume $V_1 = 1 \text{ p.u.}$ Compute V_2 and V_3 (Use Gauss-Seidel. First iteration only.)

2.) If after ten iterations of Gauss-Seidel $V_2 = 1.07 \text{ p.u.}$ and $V_3 = 0.91 \text{ p.u.}$, Compute:

2.1) Power mismatch at bus1, bus2, and bus3

2.2) Power loss of transmission systems.