# EE682 Fuel Cell Energy Processing Systems Spring 2003 <br> Prof. Ali Keyhani 

## Class Notes: DC/DC Boost Converter Design

Fuel Cells
DC/DC Converters
Inverters

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## CHAPTER 5 Boost Converter Design

### 5.1 Introduction

The Boost Converter converts an input voltage to a higher output voltage. It is also named the step-up converter. Boost converters are used in fuel cell/battery powered devices, where the load side electronic circuit requires a higher operating voltage than the source can supply.


## Figure 1 A topology of boost DC/DC converter

The transistor works as a switch which is turned on and off by a pulse-widthmodulated control voltage. The ratio between on-time and the period $t_{1} / T$ is called the Duty Cycle.

For theoretical analysis it will be assumed that the transistor is simplified as an ideal switch and the diode has no forward voltage drop. The diode will take into account a forward voltage drop $V_{\mathrm{F}}=0.7 \mathrm{~V}$.

During the on-time of the transistor, the voltage across $L$ is equal to $V_{\text {in }}$ and the current $I_{\mathrm{L}}$ increases linearly. When the transistor is turned off, the current $I_{\mathrm{L}}$ flows through the diode and charges the output capacitor. The function of the boost converter can also be described in terms of energy balance: During the on-phase of the transistor, energy is loaded into the inductor. This energy is then transferred to the output capacitor during the blocking phase of the transistor.

The output voltage is always larger than the input voltage. Even if the transistor is not switched on and off the output capacitor charges via the diode until $V_{\text {out }}=V_{\text {in }}$. When the transistor is switched the output voltage will increase to higher levels than the input voltage.

- The Boost Converter is not short circuit proof, because there is inherently no switch-off device in the short-circuit path.
A distinction is drawn between discontinuous and continuous conducing mode depending on whether the inductor current $I_{\mathrm{L}}$ reduces to zero during the off-time or not. With the help of Faraday's Law the continuous mode and steady state conditions can be established.

$$
\Delta_{\mathrm{L}}=\left(\frac{1}{L}\right) V_{\text {in }} \cdot t_{1}=\left(\frac{1}{L}\right)\left(V_{\text {out }}-V_{\text {in }}\right)\left(T-t_{1}\right)
$$

From this it follows that:

$$
V_{\text {out }}=V_{\text {in }} \cdot \frac{T}{\left(T-t_{1}\right)}
$$

- For continuous mode the output voltage is dependent on the duty cycle and the input voltage, it is independent of the load.

In discontinuous mode, the inductor current $I_{\mathrm{L}}$ will go to zero during every period. At the moment when the inductor current becomes zero, i.e. $t_{2}$, the voltage $V_{1}$ jumps to the value of $V_{\text {out }}$ because in this case $V_{\mathrm{L}}=0$. The drain-source capacitance in parallel with the diode-junction capacitance forms a resonant circuit with the inductance $L$. This is stimulated by the voltage jump across the diode. The voltage $V_{1}$ then oscillates and fades away.


Figure 2 Continuous conducing mode (CCM)


Figure 3 Discontinuous conducting mode

### 5.2 Power Switch Design

### 5.2.1 Select a power switch

BJTs (bipolar junction transistor), power MOSFETs (metal-oxide-semiconductor field effect transistors), and IGBT (insulated gate bipolar transistors) are commonly used controllable power switches (turned on/off by control signals).

BJTs and MOSFETs have characteristics that complement each other in some respects. BJTs have lower conduction losses in the ON state, especially in devices with larger blocking voltages, but have longer switching times, especially at turn-off. MOSFETs can be turned on and off much faster, but their ON state conduction losses are larger, especially in devices rated for higher blocking voltages (a few hundred volts and greater). These observations have led to attempts to combine BJTs and MOSFETs monolithically on the same silicon wafer to achieve a circuit or even perhaps a new device that combines the best qualities of both types of devices.

These attempts have led to the development of the IGBT, which is becoming the device of choice in most new applications.

In this section, design procedure will be discussed based on the difference between BJTs and MOSFETs. The methodology of using IGBT will be conceptually the same.

The criteria for choosing a power switch are the voltage and current ratings and the switching frequency. Generally, BJTs can be used for more highly rated applications than MOSFETs as shown in Figure 4

MOSFETs have higer switching frequency than BJTs. Higher frequency in power electronic circuits leads to smaller inductors and capacitors in size and weight and therefore is desired. The related details will be given in the inductor and capacitor design sections below.

BJTs are driven by base drive current $I_{B}$. The ON state base current $I_{B(s a t),}$ can be large especially in large current applications, which is not desired. MOSFETs are driven by gate-source voltage $V_{G S}$ and consumes little current. High base current leads to high loss, more complicated circuit, and more thermal concerns.


Figure 4 Votage and current ratings for BJTs and power MOSFETs
The power switch selection and design procedures will be illustrated by the following design example.

Design requirement:
A 240 -watt $\mathrm{DC} / \mathrm{DC}$ boost converter with $V_{\text {in }}=24 \mathrm{~V}$ and $V_{\text {out }}=48 \mathrm{~V}$.
Design:
Based on the circuit topology shown in Fgure 1, assuming large inductance and small current ripple, the peak transistor current should be close to the average inductor current (i.e., the input current):

$$
\mathrm{I}_{\mathrm{in}}=\mathrm{P} / \mathrm{V}_{\mathrm{in}}=240 \mathrm{~W} / 24 \mathrm{~V}=10 \mathrm{~A}
$$

Based on this current capability requirement, considering some safety margin, two candidate transistors are chosen for comparison, one is BJT 2N6547
htp://www.semi-tech-inc.com/categories php
http://www.electronica.ro/catalog/semiconductors.html
the other is power MOSFET HUFA75307D3
http://www.fairchildsemi.com/collateral/powermosfets sg.pdf
both of which satisfy the voltage and current requirement in that, for 2N6547, $\mathrm{I}_{\mathrm{C}}=15 \mathrm{~A}>10 \mathrm{~A}$ and $\mathrm{V}_{\mathrm{CE}}=400 \mathrm{~V}>48 \mathrm{~V}$, and for HUFA75307D3, $\mathrm{I}_{\mathrm{D}}=15 \mathrm{~A}>10 \mathrm{~A}$ and $\mathrm{V}_{\mathrm{DS}}=55 \mathrm{~V}>48 \mathrm{~V}$.

However, form Figure 5, t can be observed that the base current needs to be as high as 3.0A to saturate the collector which is undesirable. A BJT must work at saturation region (ON state) or cutoff region (OFF state) to be a power switch. A MOSFET is voltage driven and the threshold voltage for HUFA75307D3 is 4 V and the maximum gate-source voltage $\mathrm{V}_{\mathrm{GSmax}}=20 \mathrm{~V}$. Therefore a TTL logic +5 V or MOSFET logic +15 V circuit can be used to drive this MOSFET, which is easy for digital implementation.


Figure 5 Collector Saturation Region of 2N6547
Transient performances of these two devices need to be compared also. The rise time and fall time of 2 N 6547 are $\mathrm{t}_{\mathrm{r}}=1.0 \mu \mathrm{~s}$ and $\mathrm{t}_{\mathrm{f}}=1.5 \mu \mathrm{~s}$ for inductive load, while those of HUFA75307D3 is $\mathrm{t}_{\mathrm{r}}=40 \mathrm{~ns}$ and $\mathrm{t}_{\mathrm{f}}=45 \mathrm{~ns}$ respectively. Therefore, the power MOSFET HUFA75307D3 can be used in much higher switching frequency.

Based on the above analysis, the power MOSFET HUFA75307D3 defeats the BJT 2N6547 in performance and becomes the solution. Before the circuit is implemented, the thermal issue needs to be addressed.

The switching loss can be calculated as follows

$$
\begin{aligned}
P_{\text {loss }} & =\frac{W_{\text {loss }}^{T}=\frac{1}{T}\left(W_{\text {loss }_{-} \text {ON }}+W_{\text {loss_OFF }_{-}}\right)=\frac{V_{d s} I_{d}}{2 T}\left(t_{O N}+t_{\text {OFF }}\right)}{} \\
& =\frac{48 \times 10}{2 \times \frac{1}{20 \times 10^{3}}}(60+100) \times 10^{-9}=0.768 \mathrm{~W}
\end{aligned}
$$

The ON-state loss can be calculated as follows:

$$
\begin{aligned}
& t_{1}=\frac{1}{f}\left(\frac{V_{\text {out }}+V_{F}-V_{\text {in }}}{V_{\text {out }}}\right)=\frac{1}{20 \times 10^{3}}\left(\frac{48+0.7-24}{48}\right) \mathrm{sec}=25.73 \mu \mathrm{~s} \\
& P_{\text {ON_loss }}=\frac{W_{\text {ON_loss }}}{T}=\frac{1}{T}\left(I_{D}^{2} r_{D S(O N)} t_{1}\right) \\
& \quad=\frac{1}{\frac{1}{20 \times 10^{3}}}\left(15^{2} \times 0.075 \times 25.73 \times 10^{-6}\right)=8.684 \mathrm{~W}
\end{aligned}
$$

Therefore the overall loss $P_{\text {loss }}=P_{S W_{-} \text {loss }}+P_{\text {ON_loss }}=9.452 \mathrm{~W}<P_{D}=45 \mathrm{~W}$ (see the datasheet), where $P_{D}$ is the heat dissipation capacity of the MOSFET. From the data sheet, the maximum thermal resistance from junction-to-sink is $3.3^{\circ} \mathrm{C} / \mathrm{W}$. Therefore, the junction-to-sink temperature different is

$$
\Delta T_{j s}=R_{\theta \theta s} \times P_{\text {loss }}=3.3^{\circ} \mathrm{C} / \mathrm{W} \times 9.452 \mathrm{~W}=31.2^{\circ} \mathrm{C}
$$

According to the data sheet, the maximum operating temperature is $\mathrm{T}_{\mathrm{jmax}}=175^{\circ} \mathrm{C}$. Therefore, with right heat sink, the MOSFET will be safe. Assuming 50\% duty ratio, the transient thermal behavior can be calculated based on the normalized maximum transient thermal impedance in Fi\&ure 6 (the top curve):


Figure 6 Normalized maximum transient thermal impedance of HUFA75307D3

$$
\begin{aligned}
& \Delta T_{J C}(t)=P_{\text {loss }} Z_{\theta J C(50 \%)}(t) R_{\theta J C} \\
& \Delta T_{J C}(10 \mu s)=P_{\text {loss }} Z_{\theta J C(50 \%)}(10 \mu s) R_{\theta J C}=9.452 \mathrm{~W} \times 0.5 \times 3.3^{\circ} \mathrm{C} / \mathrm{W}=15.60^{\circ} \mathrm{C} \\
& \Delta T_{J C}(100 \mu s)=P_{\text {loss }} Z_{\theta J C(50 \%)}(100 \mu s) R_{\theta J C}=9.452 \mathrm{~W} \times 0.53 \times 3.3^{\circ} \mathrm{C} / \mathrm{W}=16.53^{\circ} \mathrm{C} \\
& \Delta T_{J C}(1 \mathrm{~ms})=P_{\text {loss }} Z_{\theta J C(50 \%)}(1 \mathrm{~ms}) R_{\theta J C}=9.452 \mathrm{~W} \times 0.63 \times 3.3^{\circ} \mathrm{C} / \mathrm{W}=19.65^{\circ} \mathrm{C} \\
& \Delta T_{J C}(10 \mathrm{~ms})=P_{\text {loss }} Z_{\theta J C(50 \%)}(10 \mathrm{~ms}) R_{\theta J C}=9.452 \mathrm{~W} \times 0.85 \times 3.3^{\circ} \mathrm{C} / \mathrm{W}=26.51^{\circ} \mathrm{C} \\
& \Delta T_{J C}(100 \mathrm{~ms})=P_{\text {loss }} Z_{\theta J C(50 \%)}(100 \mathrm{~ms}) R_{\theta J C}=9.452 \mathrm{~W} \times 1 \times 3.3^{\circ} \mathrm{C} / \mathrm{W}=31.2^{\circ} \mathrm{C}=\Delta T_{J C}(\infty)
\end{aligned}
$$

### 5.3 Inductor Design and Current Ripple Calculation

Given the following operating conditions:
$\boldsymbol{V}_{\text {in_min }}, \boldsymbol{V}_{\text {in_max }}, \boldsymbol{V}_{\text {out }}, \boldsymbol{I}_{\text {out }}$ and $\boldsymbol{f}$, where $f$ is the switching frequency.

Using these parameters, then a proposal for $L$ can be obtained:

$$
L=\left(\frac{1}{f}\right) \cdot\left(V_{\text {out }}+V_{\mathrm{F}}-V_{\text {in_min }}\right) \cdot\left(\frac{V_{\text {in_min }}}{V_{\text {out }}+V_{\mathrm{F}}}\right) \cdot\left(\frac{1}{\Delta_{\mathrm{L}}}\right)
$$

where $V_{\mathrm{F}}=0.7 \mathrm{~V}$ (Diode Forward-voltage) and $15 \%$ current ripple is assumed, i.e.,

$$
\Delta I_{L}=0.15 I_{\text {in }}=0.15 I_{\text {out }}\left(\frac{V_{\text {out }}+V_{F}}{V_{\text {in }} \min }\right)
$$

For the calculation of the curve-shapes, i.e. the peak current $I_{\max }$, two cases have to be distinguished, i.e. continuous conducting mode and discontinuous conducting mode:

$$
\begin{aligned}
& \Delta_{\mathrm{L}}=\left(\frac{1}{f}\right) \cdot\left(V_{\text {out }}+V_{\mathrm{F}}-V_{\text {in }}\right) \cdot\left(\frac{V_{\text {in }}}{V_{\text {out }}+V_{\mathrm{F}}}\right) \cdot\left(\frac{1}{L}\right) \text { and } \\
& I_{\text {in }}=I_{\text {out }} \cdot\left(\frac{V_{\text {out }}+V_{\mathrm{F}}}{V_{\text {in }}}\right)
\end{aligned}
$$

From this it follows that:
a. For $\boldsymbol{\Delta} \boldsymbol{I}_{\mathbf{L}}<\mathbf{2} \boldsymbol{I}_{\text {in }}$ the converter is in continuous mode and it follows that:

$$
\begin{aligned}
& t_{1}=\left(\frac{1}{f}\right) \cdot\left(\frac{V_{\text {out }}+V_{\mathrm{F}}-V_{\mathrm{in}}}{V_{\text {out }}}\right) \\
& \Delta I_{\mathrm{L}}=\frac{1}{L} \cdot V_{\mathrm{in}} \cdot t_{1} \text { and } \\
& I_{\max }=I_{\mathrm{in}}+\frac{1}{2} \Delta I_{\mathrm{L}}
\end{aligned}
$$

b. For $\boldsymbol{\Delta} \boldsymbol{I}_{\mathbf{L}}>\mathbf{2 I}_{\text {in }}$ the converter is in discontinuous mode and it follows that:

$$
\begin{aligned}
& t_{1}=\sqrt{2 I} \begin{array}{l}
\mathrm{out} \\
\cdot L \cdot\left(\frac{V_{\mathrm{out}}+V_{\mathrm{F}}-V_{\mathrm{in}}}{f \cdot V_{\mathrm{in}}{ }^{2}}\right) \\
t_{2}=t_{1} \cdot\left(\frac{V_{\mathrm{out}}+V_{\mathrm{F}}}{V_{\mathrm{out}}+V_{\mathrm{F}}-V_{\mathrm{in}}}\right) \text { and } \\
I_{\mathrm{max}}=\frac{1}{L} \cdot V_{\mathrm{in}} \cdot t_{1}
\end{array}, \$ \text {, }
\end{aligned}
$$

For the above design example, the required inductance can be calculated as follows:

$$
\begin{aligned}
L & =\frac{1}{f}\left(V_{\text {out }}+V_{F}-V_{\text {in }}\right)\left(\frac{V_{\text {out }}+V_{F}}{V_{\text {in }}}\right) \frac{1}{\Delta I_{L}} \\
& =\frac{1}{20 \times 10^{3}} \times(48+0.7-24) \times \frac{48+0.7}{24} \times \frac{1}{0.15 \times 10} \mathrm{H} \\
& =406 \mu \mathrm{H}
\end{aligned}
$$

Based on the inductor manufacturer MTE Corporation catalog in
able 1, onsidering the DC current capacity and some safety range, the type 18RB001 should be chosen, whose current capacity is $18 \mathrm{~A}>10 \mathrm{~A}$ and inductance is $650 \mu \mathrm{H}>406 \mu \mathrm{H}$.

The peak transistor current $\mathrm{I}_{\text {max }}$ can be calculated as follows assuming continuous conducting mode (CCM)

$$
\begin{aligned}
I_{\max } & =I_{\text {in }}+\frac{1}{2} \Delta I_{L}=I_{\text {in }}+\frac{1}{2}\left(\frac{1}{f}\right)\left(V_{\text {out }}+V_{F}-V_{\text {in }}\right)\left(\frac{V_{\text {in }}}{V_{\text {out }}+V_{F}}\right) \frac{1}{L} \\
& =10+\frac{1}{2} \frac{1}{20 \times 10^{3}}(48+0.7-24)\left(\frac{24}{48+0.7}\right) \frac{1}{650 \times 10^{-6}} \mathrm{~A} \\
& =10+0.468 \mathrm{~A}=10.468 \mathrm{~A}
\end{aligned}
$$

$\mathrm{I}_{\max }=10.468 \mathrm{~A}<15 \mathrm{~A}$, therefore the current capacity of the MOSFET meets the peak requirement.

Table 1 MTE Corporation power magnetic components - DC inductors

| $\begin{gathered} \text { DC } \\ \text { AMPS } \end{gathered}$ | $\begin{gathered} \text { INDUC. } \\ \mathbf{m H} \end{gathered}$ | CATALOG <br> No. | $\begin{gathered} \text { DC } \\ \text { AMPS } \end{gathered}$ | $\begin{gathered} \text { INDUC. } \\ \mathbf{m H} \end{gathered}$ | CATALOG <br> No. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 35.00 | 1RB001 | 40 | 0.50 | 40RB001 |
| 1 | 60.00 | 1RB002 | 40 | 0.75 | 40 RB 002 |
| 1 | 80.00 | 1RB003 | 40 | 1.00 | 40 RB 003 |
| 2 | 10.00 | 2RB001 | 40 | 2.50 | 40RB004 |
| 2 | 15.00 | 2RB002 | 50 | 0.625 | 50RB001 |
| 2 | 20.00 | 2RB003 | 50 | 0.97 | 50RB002 |
| 2 | 50.00 | 2RB004 | 50 | 1.35 | 50RB003 |
| 4 | 5.00 | 4RB001 | 50 | 2.00 | 50RB004 |
| 4 | 12.00 | 4RB002 | 62 | 0.32 | 62RB001 |
| 4 | 15.00 | 4RB003 | 62 | 0.61 | 62 RB 002 |
| 4 | 25.00 | 4RB004 | 62 | 0.67 | 62 RB 003 |
| 9 | 2.00 | 9RB001 | 62 | 1.20 | 62 RB 004 |
| 9 | 3.22 | 9RB002 | 62 | 1.50 | 62 RB 005 |
| 9 | 7.50 | 9 RB 003 | 80 | 0.31 | 80RB001 |
| 9 | 11.50 | 9 RB 004 | 80 | 0.40 | 80 RB 002 |
| 12 | 1.00 | 12RB001 | 80 | 0.50 | 80RB003 |
| 12 | 2.10 | 12 RB 002 | 80 | 0.75 | 80RB004 |
| 12 | 4.00 | 12 RB 003 | 80 | 1.25 | 80RB005 |
| 12 | 6.00 | 12RB004 | 92 | 0.20 | 92RB001 |
| 18 | 0.65 | 18RB001 | 92 | 0.60 | 92 RB 002 |
| 18 | 1.375 | 18RB002 | 92 | 1.00 | 92RB003 |
| 18 | 2.75 | 18 RB 003 | 110 | 0.25 | 110RB001 |
| 18 | 3.75 | 18RB004 | 110 | 0.30 | 110RB002 |
| 18 | 6.00 | 18RB005 | 110 | 0.45 | 110RB003 |
| 25 | 0.45 | 25RB001 | 125 | 0.11 | 125RB001 |
| 25 | 1.00 | 25RB002 | 125 | 0.22 | 125 RB 002 |
| 25 | 1.275 | 25RB003 | 125 | 0.50 | 125RB003 |
| 25 | 1.75 | 25RB004 | 125 | 0.85 | 125RB004 |
| 25 | 4.00 | 25RB005 | 150 | 0.15 | 150RB001 |
| 32 | 0.85 | 32RB001 | 150 | 0.22 | 150RB002 |
| 32 | 1.62 | 32 RB 002 | 150 | 0.32 | 150RB003 |
| 32 | 2.68 | 32 RB 003 | 150 | 0.65 | 150RB004 |


| $\begin{array}{\|c} \text { DC } \\ \text { AMPS } \end{array}$ | $\begin{array}{\|c} \text { INDUC. } \\ \mathrm{mH} \end{array}$ | CATALOG <br> No. |
| :---: | :---: | :---: |
| 200 | 0.12 | 200RB001 |
| 200 | 0.21 | 200RB002 |
| 200 | 0.40 | 200RB003 |
| 200 | 0.50 | 200RB004 |
| 240 | 0.09 | 240RB001 |
| 240 | 0.25 | 240RB002 |
| 240 | 0.35 | 240RB003 |
| 300 | 0.08 | 300RB001 |
| 300 | 0.135 | 300RB002 |
| 300 | 0.32 | 300RB003 |
| 450 | 0.055 | 450RB001 |
| 450 | 0.11 | 450RB002 |
| 450 | 0.14 | 450RB003 |
| 450 | 0.25 | 450RB004 |
| 500 | 0.043 | 500RB001 |
| 500 | 0.09 | 500RB002 |
| 500 | 0.14 | 500RB003 |
| 500 | 0.19 | 500RB004 |
| 600 | 0.04 | 600RB001 |
| 600 | 0.11 | 600RB002 |
| 600 | 0.18 | 600RB003 |
| 700 | 0.044 | 700RB001 |
| 700 | 0.06 | 700RB002 |
| 700 | 0.15 | 700RB003 |
| 850 | 0.036 | 850RB001 |
| 850 | 0.065 | 850RB002 |
| 850 | 0.11 | 850RB003 |
| 1000 | 0.02 | 1000RB001 |
| 1000 | 0.042 | 1000RB002 |
| 1000 | 0.10 | 1000RB003 |

### 5.4 Design Tips

- The larger the chosen value of the inductor $L$, the smaller the current ripple $\Delta I_{\mathrm{L}}$. However this results in a physically larger and heavier inductor.
- Choose $\Delta I_{\mathrm{L}}$ so that it is not too big. The suggestions proposed by us have adequately small current ripple along with physically small inductor size. With a
larger current ripple, the voltage ripple of the output voltage $V_{\text {out }}$ becomes clearly bigger while the physical size of the inductor decreases marginally.
- The higher the chosen value of the switching frequency $f$, the smaller the size of the inductor. However the switching losses of the transistor also become larger as $f$ increases.
- The smallest possible physical size for the inductor is achieved when $\Delta I_{\mathrm{L}}=2 I_{\text {in }}$ at $V_{\text {in_min. }}$. However, the switching losses at the transistors are at their highest in this state.


### 5.5 Capacitor Design



Figure 7 A conventional boost converter


Figure 8 Output voltage ripple

Figure 1 and Figure 1 show a conventional boost converter and the output voltage ripple and diode current, respectively. Assuming that the diode current ( $\mathrm{i}_{\mathrm{D}}$ ) is a square wave form, we can calculate the peak diode current ( $I_{D, \text { peak }}$ ) for a duty ratio of 0.5

$$
I_{D, p e a k}=\frac{I_{0}}{D}=\frac{I_{0}}{0.5}=10 \mathrm{~A}
$$

where $\mathrm{I}_{0}=\mathrm{P} / \mathrm{V}_{0}=240 / 48=5 \mathrm{~A}$ and the RMS diode current $\left(\mathrm{I}_{\mathrm{D}, \mathrm{rms}}\right)$ is

$$
I_{D, r m s}=I_{D, \text { peak }} \cdot \sqrt{D}=10 \cdot \sqrt{0.5}=7.07 \mathrm{~A}
$$

Therefore, the RMS capacitor current ( $\mathrm{I}_{\mathrm{c}, \mathrm{rms}}$ ) is given by

$$
I_{c, r m s}=\sqrt{I^{2}{ }_{D, r m s}-I^{2}{ }_{0}}=\sqrt{7.07^{2}-5^{2}}=5 \mathrm{~A}
$$

Also, the output voltage ripple can be obtained using the following equation

$$
\Delta V_{0}=\frac{\Delta Q}{C}=\frac{I_{c, r m s} D T_{s}}{C}
$$

Putting the values below into the above equation, the capacitance is

$$
\begin{aligned}
& \mathrm{D}=0.5, \mathrm{~T}_{\mathrm{s}}=1 /\left(20 \times 10^{3}\right) \mathrm{sec}, \mathrm{I}_{\mathrm{c}, \mathrm{rms}}=5 \mathrm{~A}, \Delta \mathrm{~V}_{0}=48 \mathrm{mV} . \\
& \therefore C=\frac{\Delta Q}{\Delta V_{0}}=\frac{I_{c, r m s} D T_{s}}{\Delta V_{0}}=\frac{5 \cdot 0.5}{48 \times 10^{-3} \times 20 \times 10^{3}}=2600 \mu F
\end{aligned}
$$

Therefore, the capacitor should be selected based on the rated voltage, the rated ripple current, and the capacitance calculated above. Finally, we chose the rated voltage $(100 \mathrm{~V})$ considering over-voltage by a parasite inductance, the rated ripple current (at least 5 A ), and the capacitance (at least $2600 \mu \mathrm{~F}$ ).

Next, we have to choose the supplier that manufactures the capacitors with the above specifications. In this case, we choose the Aluminum Electrolyte Capacitor manufactured by Sam Young Electronics Co., and the list of products is given below.

Table 2 List of Aluminum Electrolyte Capacitors

## LIST OF PRODUCTS

## MINIATURE ALUMINUM ELECTROLYTIC CAPACITORS

| Series |  |  | Applications | $\begin{aligned} & \text { Load } \\ & \text { life } \\ & \text { Time } \\ & \text { (Hrs) } \end{aligned}$ |  |  |  |  |  | Terminal type | Roted voltage range (VDC) | Capacitance range ( $\mu \mathrm{F}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | General <br> Purpose | MV | $5.5 \sim 10.5 \mathrm{~mm}$ max.height | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 1000 \sim 200 \mathrm{hrs} \end{gathered}$ |  | - |  |  | - | SMD | 4~50 | $0.1 \sim 1.000$ |
|  |  | MVG | $5.5 \sim 6.0 \mathrm{~mm}$ max. height, downsized | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  | - | SMD | 4~50 | $0.1 \sim 220$ |
|  |  | $\frac{M V K}{d i v}$ | $\begin{aligned} & 5.5 \sim 10.5 \\ & \text { mm } \\ & \text { max.height } \end{aligned}$ | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 1000 \sim 200 \mathrm{hrs} \end{gathered}$ |  | - |  | - | - | SMD | $6.3 \sim 50$ | $0.1 \sim 1,000$ |
|  |  | MVY | $5.5 \sim 10.5$ mm max.height, Low Imp | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 1000 \sim 200 \mathrm{hrs} \end{gathered}$ |  |  | - | - | - | SMD | 6.3~35 | 4.7~470 |
|  | Bi-Polar | MV-BP | 5.5 mm max. height, Bi-polar | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  |  |  |  | - | SMD | 4~50 | 0.1~47 |
|  |  | MVK-BP | 6.0 mm max height, Bi-polar | $105^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  |  |  | - | - | SMD | 6.3~50 | $0.1 \sim 47$ |
|  | Low Profile | SRE | 5 mm height | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  | - |  |  |  | Radial | 4~50 | $0.1 \sim 330$ |
|  |  | SRA | 7 mm height | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  | - |  |  |  | Radial | 4~63 | $0.1 \sim 220$ |
|  |  | $\frac{\text { GSA }}{\text { (NEW) }}$ | 7 mm height, downsized | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  |  | Radial | 6.3~50 | $0.1 \sim 220$ |
|  |  | KRE | 5 mm height, Wide temp | $105^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  | - | - |  | - | Radial | 4~50 | $0.1 \sim 100$ |
|  |  | KMA | 7 mm height | $105^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  | - | - |  | - | Radial | 4~63 | $0.1 \sim 150$ |
|  |  | SR | $9 \sim 16 \mathrm{~mm}$ height | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  |  | Radial | 4~50 | 22~1,000 |
|  | General Purpose | SHL | General | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - | - |  |  |  | Radial | $6.3 \sim 450$ | $0.1 \sim 15,000$ |
|  |  | $\frac{\text { MHA }}{\text { (NEW) }}$ | High capacitance | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  |  | Radial | 160~450 | 1~820 |
|  |  | KMG | General | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 1000 \sim 200 \mathrm{hrs} \end{gathered}$ | - | - |  |  | - | Radial | $6.3 \sim 450$ | 0.1~15,000 |
|  |  | $\frac{\mathrm{NHA}^{(N)}}{(\mathrm{NEW})}$ | High capacitance | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 1000 \sim 200 \mathrm{hrs} \end{gathered}$ | - |  |  |  |  | Radial | 160~450 | 1~680 |
|  | Low Leakage | SRA-LL | Height 7mm | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  |  | Radial | 6.3~50 | $0.1 \sim 100$ |
|  |  | LL | General | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  | - |  |  |  | Radial | $6.3 \sim 100$ | 0.1~4,700 |
|  | Bi-polar | SRE-BP | 5 mm height | $85^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ | $\bigcirc$ |  |  |  |  | Radial | 4~50 | $0.1 \sim 47$ |
|  |  | SRA-BP | 7 mm height | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ | - |  |  |  |  | Radial | $6.3 \sim 50$ | 0.1~47 |
|  |  | SHL-BP | General | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  | - |  |  |  | Radial | $6.3 \sim 250$ | 0.47~6,800 |
|  |  | KMG-BP | General, Wide temp | $105^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  | - |  | - | - | Radial | $6.3 \sim 250$ | 0.47~6,800 |
|  |  | SSP | Speaker Network | $85^{\circ} \mathrm{C} 2000 \mathrm{hrs}$ |  | - |  |  |  | Radial | 25~63 | 1~100 |
|  |  | SSA | Horizontal deflection | $85^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  | - |  |  |  | Radial | 25, 50 | 2.2~10 |
|  |  | KSA | Horizontal deflection | $105^{\circ} \mathrm{C} 1000 \mathrm{hrs}$ |  |  |  | - | - | Radial | 25, 50 | 2.2~10 |



## LARGE SIZED ALUMINUM ELECTROLYTIC CAPACITORS

| S | Series |  | Applications | Load life Time (Hrs) |  | Standard type |  | $\qquad$ | $\overline{8}$ 훈 $\dot{4}$ ㅎ i | Terminal type | Roted voltage range (VDC) | Capacitance range ( $\mu \mathrm{F}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | General Purpose | SMH | General | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 200 \mathrm{hrs} \end{gathered}$ |  | - |  |  |  | Pin | 100~500 | 56~82,000 |
|  |  | RDA | Miniature | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ | - |  |  |  |  | Pin | 160~450 | 68~2,700 |
|  |  | KMH | General, Wide temp | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ |  | $\bigcirc$ |  | - |  | Pin | 16~450 | 56~47,000 |
|  |  | TDA | Miniature | $\begin{aligned} & 105^{\circ} \mathrm{C} \\ & 2000 \mathrm{hrs} \end{aligned}$ | $\bigcirc$ |  |  | - |  | Pin | 160~450 | 56~2,200 |
|  |  | SLT | 20 mm height | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ | - |  |  |  |  | Pin | 160~400 | 47~560 |
|  |  | KLT | 20 mm height | $\begin{aligned} & 105^{\circ} \mathrm{C} \\ & 2000 \mathrm{hrs} \end{aligned}$ | $\bigcirc$ |  |  | - |  | Pin | 160~400 | 47~560 |
|  |  | LXG | Miniature long life | $\begin{aligned} & 105^{\circ} \mathrm{C} \\ & 5000 \mathrm{hrs} \end{aligned}$ | $\bigcirc$ |  |  | - |  | Pin | 10~400 | 56~47,000 |
|  | Special Application | KLG | No spark with DC overvoltage | $\begin{gathered} 105^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ | ) |  |  |  |  | Pin | 200, 400 | 47~1,500 |
|  |  | DL | General Audio | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ |  | - |  |  |  | Pin | 50~100 | 3,300~22,000 |
|  |  | AHS | Hi-Fi Audio Miniature | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ | $\bigcirc$ |  |  |  |  | Pin | 50~100 | $3.300 \sim 22,000$ |
| $\stackrel{\text { ® }}{\stackrel{\text { D }}{2}}$ | General Purpose | SME | General | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ |  | - |  |  |  | Screw | 10~250 | 560~680,000 |
|  |  | $\underline{\mathrm{KMH}}$ | General, wide temp. | $\begin{aligned} & 105^{\circ} \mathrm{C} \\ & 2000 \mathrm{hrs} \end{aligned}$ |  | $\bigcirc$ |  | - |  | Screw | 10~400 | 180~680,000 |
|  | For Inverter | RWA | High ripple | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 2000 \mathrm{hrs} \end{gathered}$ |  | $\bigcirc$ |  |  |  | Screw | 350, 400 | 270~10,000 |
|  |  | RWF | High ripple, long life | $\begin{gathered} 85^{\circ} \mathrm{C} \\ 5000 \mathrm{hrs} \end{gathered}$ |  |  |  | $\bigcirc$ |  | Screw | 350~450 | 2,700~15.000 |
|  | Special Application | PH | For Photo Flash | $\begin{gathered} 5 \sim 35^{\circ} \mathrm{C} \\ 5,000 \\ \text { times } \end{gathered}$ |  |  |  |  |  | Pin/ | 330 | 165~2,000 |
|  |  | DH | For Welding | $\begin{gathered} 40^{\circ} \mathrm{C} \\ 1,000,000 \\ \text { times } \end{gathered}$ |  |  |  |  |  | Screw | 315,475 | 100~330 |

In general, the price of capacitors is determined by the order of rated voltage, capacitance, maximum permissible ripple currents, maximum permissible temperature, and ESR (Equivalent Series Resistance). Therefore, designers have to choose the optimal type that can satisfy the requirements such as cost, permissible temperature, size, and ESR, etc. In this case, we selected KMH series used for General Purpose from the above catalog.

The below table shows only the information required for selection of our capacitor in full data sheets of KMH series. From "table of permissible ripple current", we have to consider a factor by switching frequency and case diameter when we calculate the maximum permissible currents. So, we selected $\Phi 35$ of rated voltage 100 V , and we have to multiply a factor (1.3) by the permissible ripple current (from table of "rating of KMH series") because the switching frequency is 20 kHz .

Table 3 Data sheet of KMH Series


PERMISSIBLE RIPPLE CURRENT
Frequency Multiplying Factor


RATINGS OF KMH Series

| ${ }_{\mu F}^{\mathrm{VDC}}$ | 100(2A) |  |  | 160(2C) |  |  | $20012 \mathrm{D})$ |  |  | 260(2E) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 180 |  |  |  |  |  |  |  |  |  |  |  |  |
| 220 |  |  |  |  |  |  |  |  |  |  |  |  |
| 270 |  |  |  |  |  |  |  |  |  | A6 | 0.8 | 0.15 |
| 330 |  |  |  |  |  |  | A5 | 0.9 | 0.16 | A6 | 0.9 | 0.16 |
| 390 |  |  |  |  |  |  | A5 | 1.0 | 0.15 | А6 | 1.0 | 0.15 |
| 470 |  |  |  |  |  |  | A5 | 1.1 | 0.16 | А6 | 1.1 | 0.15 |
| 560 |  |  |  | A5 | 1.2 | 0.15 | А5 | 1.2 | 0.16 | A6 | 1.2 | 0.15 |
| 680 |  |  |  | A5 | 1.3 | 0.15 | A5 | 1.3 | 0.16 | A6 | 1.4 | 0.15 |
| 820 |  |  |  | A5 | 1.4 | 0.15 | A5 | 1.4 | 0.15 | A8 | 1.6 | 0.15 |
| 1,000 |  |  |  | A5 | 1.6 | 0.15 | A6 | 1.7 | 0.15 | As | 1.6 | 0.20 |
| 1,200 |  |  |  | A6 | 1.9 | 0.15 | A6 | 1.9 | 0.16 | A8 | 1.8 | 0.20 |
| 1,500 |  |  |  | A6 | 2.1 | 0.15 | A8 | 2.3 | 0.15 | A10 | 2.1 | 0.20 |
| 1,800 | A5 | 2.7 | 0.10 | $A B$ | 2.5 | 0.15 | AB | 2.5 | 0.16 | A12 | 2.5 | 0.20 |
| 2,200 | A5 | 3.0 | 0.10 | A8 | 2.8 | 0.15 | A10 | 2.5 | 0.16 | A12 | 2.5 | 0.20 |
| 2,700 | A6 | 3.5 | 0.10 | A10 | 3.3 | 0.15 | A12 | 3.6 | 0.15 | C10 | 3.5 | 0.20 |
| 3,300 | A8 | 4.2 | 0.10 | A12 | 3.8 | 0.15 | CB | 4.1 | 0.15 | C12 | 4.2 | 0.20 |
| 3,900 | A8 | 4.2 | 0.12 | 8 | 3.8 | 0.20 | C10 | 4.9 | 0.15 | C12 | 4.6 | 0.20 |
| 4,700 | A10 | 5.0 | 0.12 | C10 | 4.6 | 0.20 | D10 | 6.3 | 0.20 | D12 | 6.7 | 0.20 |
| 5,600 | A10 | 5.4 | 0.12 | C10 | 5.1 | 0.20 | D10 | 6.8 | 0.20 | D12 | 6.3 | 0.20 |
| 6,800 | A12 | 5.8 | 0.15 | C12 | 6.1 | 0.20 | D12 | 6.9 | 0.20 | E12 | 7.7 | 0.20 |
| 8,200 | $\mathrm{C8}$ | 6.4 | 0.15 | D10 | 7.0 | 0.20 | D12 | 7.6 | 0.20 | E12 | 8.4 | 0.20 |
| 10,000 | C10 | 7.8 | 0.15 | D12 | 8.4 | 0.20 | E12 | 9.3 | 0.20 | E14 | 10.0 | 0.20 |
| 12,000 | C12 | 9.3 | 0.15 | E10 | 9.4 | 0.20 | E12 | 10.2 | 0.20 | F14 | 11.9 | 0.20 |
| 15,000 | C12 | 10.4 | 0.15 | E12 | 11.4 | 0.20 | E12 | 10.2 | 0.20 | F14 | 11.9 | 0.20 |
| 18,000 | D10 | 10.4 | 0.20 | E14 | 13.4 | 0.20 | F14 | 13.1 | 0.25 |  |  |  |
| 22,000 | D12 | 12.5 | 0.20 | F14 | 14.5 | 0.25 |  |  |  |  |  |  |
| 27,000 | E12 | 13.7 | 0.25 | F14 | 16.0 | 0.25 |  |  |  |  |  |  |
| 33,000 | E12 | 16.2 | 0.25 |  |  |  |  |  |  |  |  |  |
| 39,000 | E14 | 16.1 | 0.30 |  |  |  |  |  |  |  |  |  |
| 47,000 | F14 | 19.3 | 0.30 |  |  |  |  |  |  |  |  |  |
| 56,000 | F14 | 21.1 | 0.30 |  |  |  |  |  |  |  |  |  |

- Permissible Ripple Current(Arms / 105 C , 120 Hz )

A Case Code

Based on the above table ("Rating of KMH Series") and our requirements, even if we can choose any capacitor above $3300 \mu \mathrm{~F} / 4.2 \mathrm{~A}$ in 100 V rated voltage, we selected a 3900 $\mu \mathrm{F} / 4.2$ A because we have to consider ESR.

- Capacitance: $3900 \mu \mathrm{~F}>2600 \mu \mathrm{~F}$
- Maximum permissible ripple current: $4.2 \times 1.3=5.46 \mathrm{Arms}>5 \mathrm{~A}$

Therefore, our design is reasonable by conditions above.

## Bibliography

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