## EE341 - Course Notes Electric Circuit Analysis

## Homework No. 1

Instructor: Ali Keyhani

## Homework No. 1

1. The operation of AC machines (in particular, transformers and induction machines) can be studied with the aid of the T-Circuit shown below.


## Homework No. 1

Several parameter sets are given in the table below. Your solutions should be summarized in a table in format as shown below. Use polar form for all complex number. Show your calculations separately.

| Set | $\mathrm{V}_{1}$ | $\mathrm{~V}_{2}$ | $\mathrm{I}_{1}$ | $\mathrm{I}_{2}$ | $\mathrm{I}_{\mathrm{f}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Example 1 | $2700 \angle 22^{\circ}$ | - | $10 \angle-39^{\circ}$ | $10 \angle-39^{\circ}$ | 0 |
| Example 2 | - | $23 \angle-54.6^{\circ}$ | $259.4 \angle-54.6^{\circ}$ | $259.4 \angle-54.6^{\circ}$ | $23 \angle-55^{\circ}$ |

(Example solution)

## Homework No. 1

## Practice all cases.

Only cases with parametes sets $1,2,4$, and 11 will be graded.
Write a Matlab program to solve case 11.

| S | $\mathrm{Z}_{1}$ |  | $\mathrm{Z}_{\phi} \quad$ Parallel |  | $\mathrm{Z}_{2}$ |  | $\mathrm{Z}_{\mathrm{L}}$ |  | V1 | V2 | $\mathrm{I}_{1}$ | $\mathrm{I}_{2}$ | $I_{f}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| T | $\mathrm{R}_{1}$ | $\mathrm{L}_{1}$ | $\mathrm{R}_{\mathrm{f}}$ | $\mathrm{L}_{\mathrm{m}}$ | $\mathbf{R}^{\prime}{ }_{2}$ | $\mathrm{L}^{\prime}{ }_{2}$ | $\mathbf{R}_{\mathrm{L}}$ | $L_{L}$ |  |  |  |  |  |
| 1 | 1 | 0.01 | 10000 | 8 | 1 | 0.01 | Open Circuit |  | $\begin{aligned} & 480 \angle \\ & 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |
| 2 | 1 | 0.01 | 10000 | 8 | 1 | 0.01 | 200 | 0 | $\begin{aligned} & 480 \angle \\ & 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |
| 3 | 0.02 | 0.00265 | Open Circuit |  | 0 | 0 | Open Circuit |  | $1 \angle 0^{\circ}$ | ? | $?$ | ? | ? |
| 4 | 0.02 | 0.00265 | Open Circuit |  | 0 | 0 | 1.0 | 0 | $1 \angle 0^{\circ}$ | ? | ? | ? | ? |
| 5 | 0.02 | 0.00265 | Open Circuit |  | 0 | 0 | . 707 | $\begin{aligned} & 1.875 x \\ & 10^{-3} \end{aligned}$ | ? | $1 \angle 0^{\circ}$ | ? | ? | ? |
| 6 | 0 | 0 | 100 | 0.1 | 0.01 | $\begin{aligned} & 106 x \\ & 10^{-6} \end{aligned}$ | 1.0 | 0 | $1 \angle 0^{\circ}$ | ? | $?$ | ? | ? |

## Homework No. 1

| $\begin{aligned} & \mathrm{S} \\ & \mathrm{E} \end{aligned}$ | $\mathrm{Z}_{1}$ |  | $\mathrm{Z}_{\phi} \quad$ Parallel |  | $\mathrm{Z}^{\prime}$ |  | $\mathrm{Z}_{\mathrm{L}}$ |  | V1 | V2 | $\mathrm{I}_{1}$ | $\mathrm{l}_{2}$ | $\mathrm{If}_{f}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{R}_{1}$ | $\mathrm{L}_{1}$ | $\mathrm{R}_{\mathrm{f}}$ | $\mathrm{L}_{\mathrm{m}}$ | $\mathrm{R}^{\prime}{ }_{2}$ | $\mathrm{L}^{\prime}$ | $\mathrm{R}_{\mathrm{L}}$ | $\mathrm{L}_{\mathrm{L}}$ |  |  |  |  |  |
| 7 | 0 | 0 | 100 | 0.01 | . 01 | $\begin{aligned} & 106 \\ & \times 10^{-6} \end{aligned}$ | 1.414 | $\begin{aligned} & 3.75 \times 1 \\ & 0^{-3} \end{aligned}$ | $1 \angle 0^{\circ}$ | ? | ? | ? | ? |
| 8 | . 3 | $\begin{aligned} & 1.33 x \\ & 10^{-3} \end{aligned}$ | Open <br> Circuit | $\begin{aligned} & 3.45 \\ & \times 10^{-2} \end{aligned}$ | . 15 | $\begin{aligned} & .56 \\ & \times 10^{-3} \end{aligned}$ | 7.35 | 0 | $\begin{aligned} & 127 \\ & \angle 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |
| 9 | 10 | $\begin{aligned} & 5.2 \\ & \times 10^{-2} \end{aligned}$ | Open Circuit |  | 0 | 0 | 200 | . 4 | ? | $\begin{aligned} & 5000 \\ & \angle 0^{\circ} \end{aligned}$ | ? | ? | ? |
| 10 | . 15 | $\begin{aligned} & 2.54 x \\ & 10^{-3} \end{aligned}$ | Open Circuit |  | 1.57 | $\begin{aligned} & 6.24 x \\ & 10^{-3} \end{aligned}$ | 98.5 | . 178 | $\begin{aligned} & 2400 \\ & \angle 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |
| 11 | . 3 | 0.003 | 1 | $\begin{aligned} & 4.25 \\ & \times 10^{-2} \end{aligned}$ | . 2 | . 003 | 10 | 0 | $\begin{aligned} & 440 \\ & \angle 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |
| 12 | . 3 | 0.003 | 0 | ${ }_{-2} 4.25 \times 10$ | . 2 | . 003 | 1.0 | 0 | $\begin{aligned} & 380 \\ & \angle 0^{\circ} \end{aligned}$ | ? | ? | ? | ? |

## Homework No. 1

## Assume

1. All elements are in series except $R_{f}$ and $L_{m}$ which are in parallel.
2. $\mathbf{R}=$ ohms; L=henrys; $\mathrm{V}=$ volts; $\omega \mathrm{L}=\mathrm{ohms}$.
3. $\omega=\mathbf{2} \pi \mathrm{f}=\mathbf{3 7 7}$ radsec; $\mathrm{jX}=\mathrm{j} \omega \mathrm{L}$ for $\mathrm{f}=\mathbf{6 0 H z}$
4. Open circuit $=R$ and/or $L$ to infinity
5. Short circuit $=\mathbf{R}$ and/or $L$ to $\rightarrow \mathbf{0}$

## Homework No. 1

2. For the cases with parameters sets 1, 2, 4 and 11 in the table, draw the Thevenin equivalent circuits seen by the load Impedance $Z_{L}{ }^{\prime}$, connected to terminals A-B. Calculate the parameters of the Thevenin equivalents circuits.
3. For cases with parameter sets 1, 2, 4 and 11 in the table, and assuming $L_{L}{ }^{\prime}=0$. Find the values of $R_{L}$ ' wich will result in the maximum power delivered to $\mathrm{R}_{\mathrm{L}}{ }^{\prime}$. (use the maximum power transfer principle).
4. As the power specialist in your company, you are asked to derive a model of an AC machine. With the machine terminals opencircuited, you are measure Voc=100V. With the machine terminals shorted, you measure Isc=50A. Calculate the parameters of the Thevenin Equivalent circuit of the machine.
